

**Module II, Course Activity 1: Antiderivatives and the First FTC**  
**Synthesis Questions**

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Name: \_\_\_\_\_

*Procedure:* Complete the following synthesis questions. Attach any extra pages of work, explanations, and answers.

Using the (First) Fundamental Theorem of Calculus:

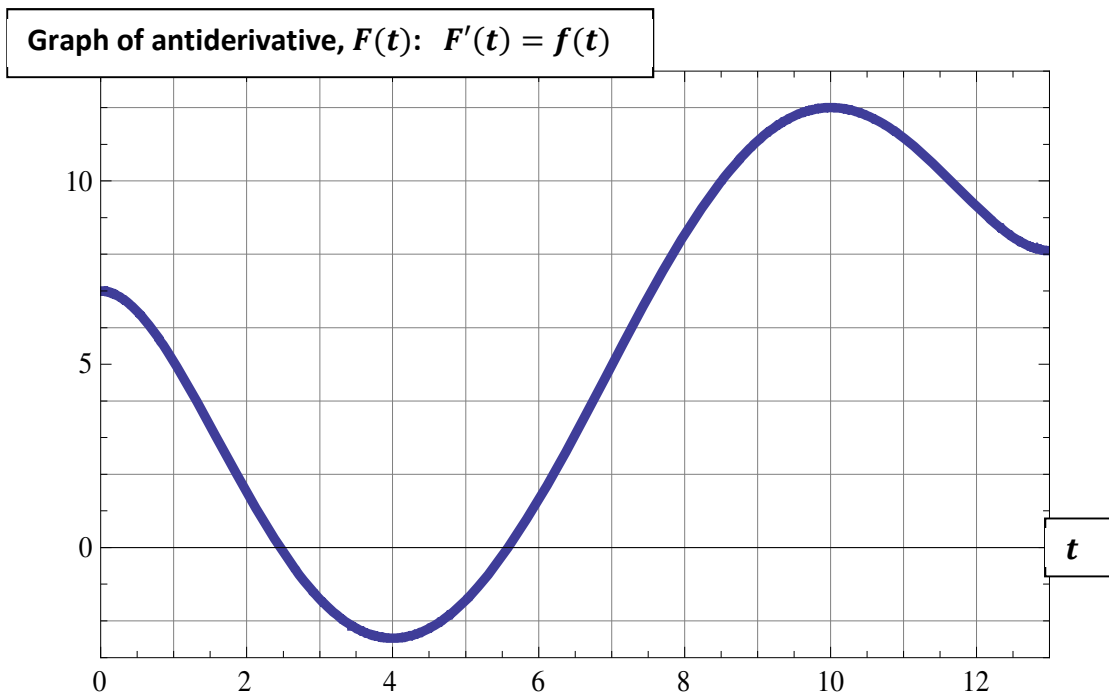
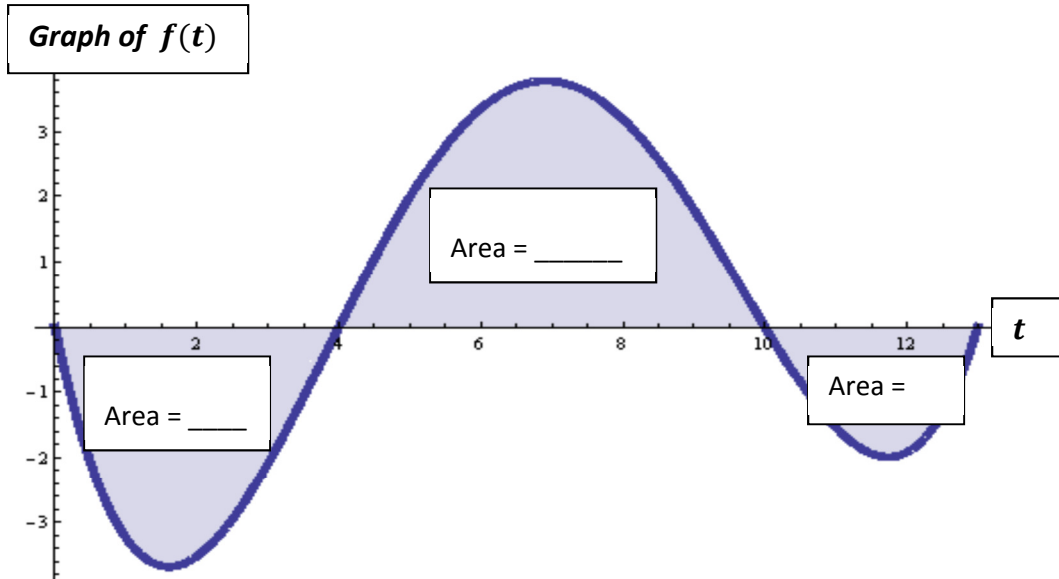
**Numerical Problems:**

1. Some values for a continuous function  $g(x)$  are given in the second row of the table below.  $G(x)$  is an antiderivative of  $g(x)$ . The initial value for  $G(x)$  is given. Compute approximate values for  $G(x)$  to fill in the rest of the third row of the table below. Show all of your computations and indicate how the (First) Fundamental Theorem of Calculus is being used.

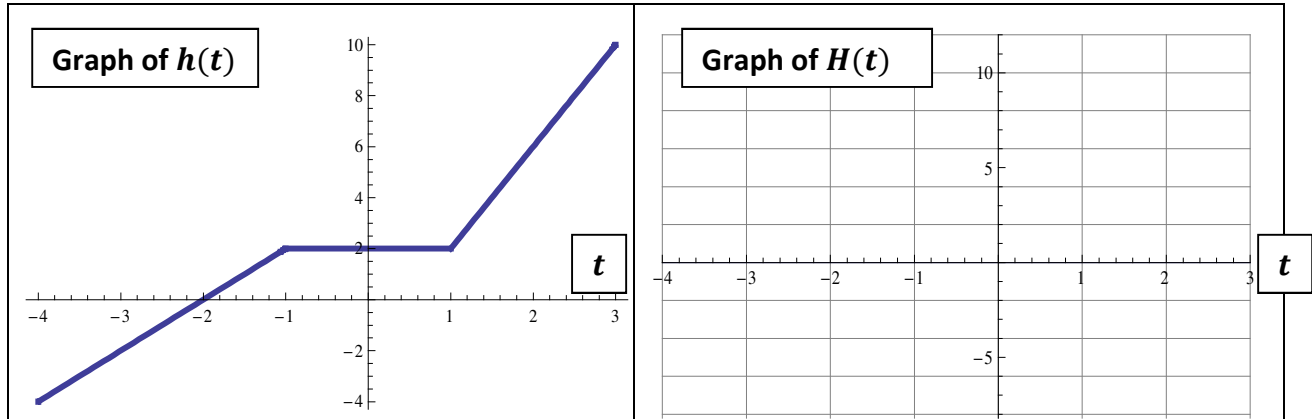
$x$	<b>0</b>	<b>4</b>	<b>8</b>	<b>12</b>	<b>16</b>
$g(x)$	3	6	7	5	2
$G(x)$	11				

**Graphical Problems:** Use the (First) Fundamental Theorem of Calculus to answer the following graphical questions as accurately as possible.

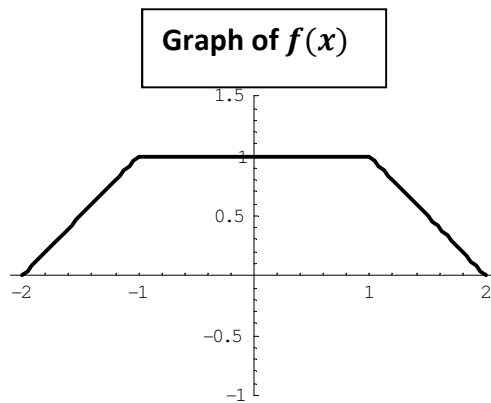
2. Consider the graphs below. On top is the graph of a function  $f(t)$  and below that, one of its antiderivatives,  $F(t)$ , is graphed. Fill in the missing areas of the shaded regions.



3. The graph of a function,  $h(t)$ , is given on the left below. Sketch an accurate graph of the antiderivative,  $H(t)$ , ( $H'(t) = h(t)$ ), with  $H(-4) = -2$ . Indicate specific values for  $H(t)$  on your graph at each integer value of  $t$ , by locating those points correctly on the grid, and/or writing the ordered pairs on the graph.

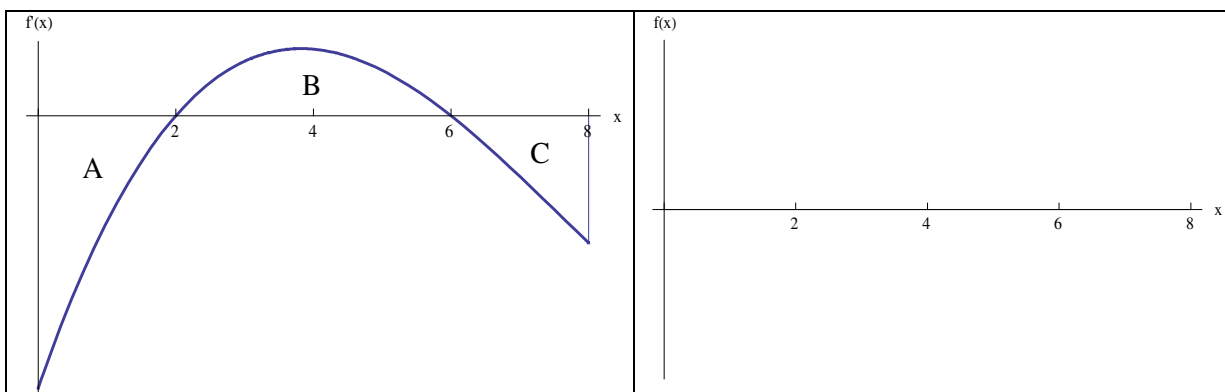


4. Consider the graph of a function  $f(x)$  given below:



- If  $F(x)$  is an antiderivative of  $f(x)$  and  $F(-2) = 0$ , compute  $F(0)$ .
- If  $F(x)$  is an antiderivative of  $f(x)$  and  $F(-1) = -2$ , compute  $F(2)$ .

5. The graph of a derivative function,  $f'(x)$ , is shown on the left below.



- a. Sketch a possible graph of the function  $f(x)$  on the blank axes to the right above.
- b. If the areas of the regions labeled in the graph of  $f'(x)$  are: area of region A = 5, area of region B = 4, and area of region C = 3, and if  $f(0) = 8$ , then find the following values of  $f(x)$ :
- $f(2) = \underline{\hspace{2cm}}$        $f(6) = \underline{\hspace{2cm}}$        $f(8) = \underline{\hspace{2cm}}$
6. The family of all antiderivatives of a function,  $f(x)$ , is called the **indefinite integral** of  $f$  and is denoted by  $\int f(x)dx$ . Find the following indefinite integrals:
- a.  $\int(4x^2 - 17x + 2\sqrt{x}) dx =$
- b.  $\int \sin(4x) dx =$
- c.  $\int e^{3x} dx =$
- d.  $\int \frac{4}{x} dx =$
7. Describe the difference between the *definite integral*,  $\int_2^5 3x^5 dx$  and the *indefinite integral*,  $\int 3x^5 dx$ .